

Refraction and Total Internal Reflection

Matthew Williams • Physics • May 20, 2026

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Refraction

Refraction is the change in direction of a wave when it passes from one medium into another in which its speed is different. Light bends toward the normal when it slows down (entering a denser medium) and away from the normal when it speeds up (entering a less dense medium).

Normal incidence (90° to the boundary) produces no bending.

Snell's Law

$$\frac{\sin i}{\sin r} = n$$

where i is the angle of incidence, r

is the angle of refraction (both measured from the normal), and n is the **refractive index** of the second medium relative to the first (e.g. relative to air).

The refractive index is also related to wave speed:

$$n = \frac{c}{v}$$

where c is the speed of light in air (or vacuum) and v

is the speed of light in the medium. A medium with a higher refractive index has a lower speed of light.

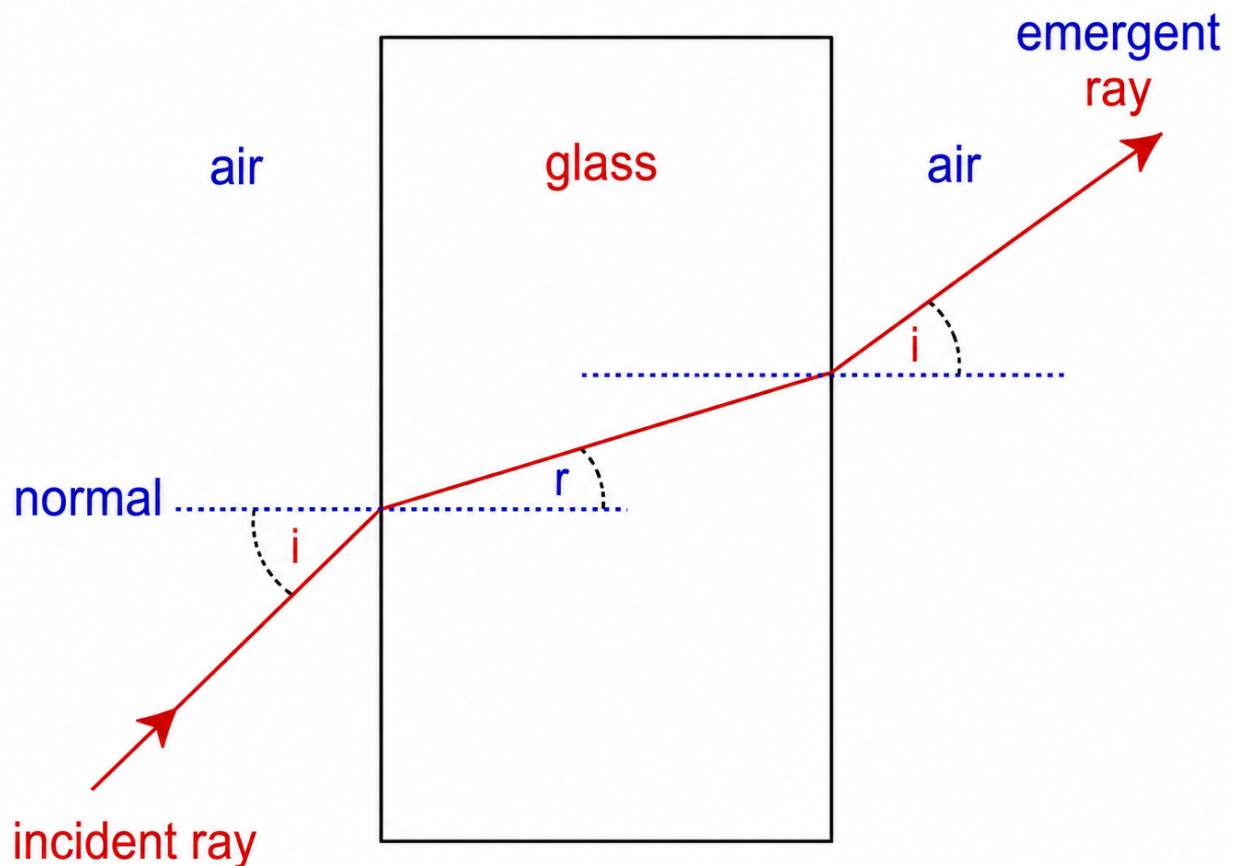


Diagram showing a light ray striking a rectangular glass block (a denser medium) from air: the ray bends toward the normal on entering the glass, with the angle of incidence i in air larger than the angle of refraction r in glass; the ray travels straight through the block and exits at the opposite face, bending away from the normal to produce an emergent ray that is parallel to the original incident ray

Real and Apparent Depth

When an object at the bottom of a pool of water is viewed from above, it appears closer to the surface than it really is, refraction at the water-air interface bends the light outward. The apparent depth is less than the real depth:

$$n = \frac{\text{real depth}}{\text{apparent depth}}$$

A coin at the bottom of a 1.3 m pool ($n = 1.3$) appears to be at depth $1.3/1.3 = 1.0$ m.

Critical Angle and Total Internal Reflection

When light travels from a denser medium to a less dense medium (e.g. from glass to air), the refracted ray bends away from the normal. As the angle of incidence increases, so does the angle of refraction.

At the **critical angle C**

, the refracted ray travels along the boundary (angle of refraction = 90°). Beyond the critical angle, no refraction occurs, all light is reflected back into the denser medium. This is

total internal reflection (TIR).

$$\sin C = \frac{1}{n}$$

Two conditions for TIR:

- 1. Light must be travelling from a denser medium to a less dense medium.
- 2. The angle of incidence must be greater than the critical angle.

<TotalInternalReflectionDiagram />

Applications of Total Internal Reflection

Optical Fibres

Optical fibres are thin strands of glass or plastic. Light entering one end hits the curved walls at angles greater than the critical angle and is totally internally reflected along the fibre, even around bends. The light exits at the other end with very little loss.

Applications: telecommunications (internet cables), endoscopy (medical imaging of the inside of the body).

Right-Angle Prism

A glass prism (refractive index approximately 1.5, critical angle approximately 42°) can totally internally reflect light at its 45° face, since $45^\circ > 42^\circ$. Two prisms can form a periscope or binoculars without the need for mirrors, with no light loss.

Refraction and critical angle calculations (2023 Paper 02, Q3)

The refractive index of water is 1.3. The speed of light in air is $3 \times 10^8 \text{ m s}^{-1}$.

Speed of light in water:

$$v = \frac{c}{n} = \frac{3 \times 10^8}{1.3} \approx 2.31 \times 10^8 \text{ m s}^{-1}$$

Critical angle of water:

$$\sin C = \frac{1}{n} = \frac{1}{1.3} = 0.769$$

$$C = \sin^{-1}(0.769) \approx 50.3^\circ$$

Light inside water hitting the surface at angles greater than 50.3° is totally internally reflected.

Refraction through ice (2021 Paper 02, Q3)

Light enters a cube of ice at face MN. The refractive index of ice is 1.31. The angle of incidence on face MN is 30° .

Angle of refraction:

$$\sin r = \frac{\sin i}{n} = \frac{\sin 30^\circ}{1.31} = \frac{0.500}{1.31} \approx 0.382$$

$$r = \sin^{-1}(0.382) \approx 22.4^\circ$$

Light bends toward the normal on entering the denser ice.

Exam Tip

The critical angle formula $\sin C = 1/n$

only applies when going from the denser medium to air (or vacuum). For the derivation: at the critical angle, the angle of refraction is exactly 90° , so Snell's Law gives

$n \sin C = 1 \times \sin 90^\circ = 1$, hence $\sin C = 1/n$.

Always state the two conditions for total internal reflection together: denser to less dense medium, AND angle of incidence exceeds the critical angle.